

Section – A

1. (A)

By remainder theorem,

$$P\left(-\frac{1}{2}\right) = -1$$

$$\therefore 4\left(-\frac{1}{2}\right)^3 - k\left(-\frac{1}{2}\right)^2 - \frac{1}{2} - 7 = -1$$

$$\therefore -\frac{1}{2} - \frac{k}{4} - \frac{15}{2} = -1$$

$$\therefore k = -28$$

2. (D)

$$\text{Let } u = \frac{1}{7x-4y} \text{ and } v = \frac{1}{4x-7y}$$

$$\therefore 4u + 10v = -5 \text{ and } 3u - 10v = -2$$

$$\text{On solving we get, } u = -1 \text{ and } v = \frac{-1}{10}$$

$$\therefore 7x - 4y = -1 \text{ and } 4x - 7y = -10$$

$$\text{On solving we get, } x = 1 \text{ and } y = 2$$

$$\therefore x^2 + y^2 = 1^2 + 2^2 = 5$$

3. (B)

$$|-4x + 3| = \frac{1}{2} \Rightarrow -4x + 3 = \pm \frac{1}{2} \Rightarrow -4x = -\frac{5}{2}, -\frac{7}{2} \Rightarrow x = \frac{5}{8}, \frac{7}{8}$$

$$\therefore \frac{5}{8} + \frac{7}{8} = \frac{12}{8} = \frac{3}{2}$$

4. (A)

$$x = 1 + 2^{1/3} + 2^{2/3}$$

$$\therefore (x-1)^3 = (2^{1/3} + 2^{2/3})^3$$

$$\therefore (x-1)^3 = 6 + 6(x-1)$$

$$\therefore x^3 - 3x^2 - 3x = 1$$

5. (C)

By remainder theorem,

$$P(3) = 2 \text{ and } P(2) = 3$$

$$\text{Also, } P(x) = Q(x)(x-2)(x-3) + ax + b$$

$$\therefore P(3) = 3a + b = 2 \text{ and } P(2) = 2a + b = 3$$

On solving we get, $a = -1$ and $b = 5$

$$\therefore \text{Remainder} = ax + b = -x + 5$$

6. (D)

$$x^2 - 4x + k = (x - \alpha)(x - \beta)$$

$$\therefore \alpha + \beta = 4 \text{ and } \alpha\beta = k$$

$$2\alpha + 3\beta = 10$$

On solving we get, $\alpha = \beta = 2$

$$\therefore k = \alpha\beta = 4$$

7. (A)

$$\left(\sqrt{x} + \frac{1}{\sqrt{x}}\right)^2 = x + \frac{1}{x} + 2 \text{ and } \left(x + \frac{1}{x}\right)^2 = x^2 + \frac{1}{x^2} + 2$$

$$\therefore x + \frac{1}{x} = \pm 3 \quad \therefore \sqrt{x} + \frac{1}{\sqrt{x}} = \pm\sqrt{5}$$

8. (B)

$y = p(x)$ intersects X-axis 3 times.

9. (C)

$$x^4 + 2x^2 + 9 = x^4 + 6x^2 + 9 - 4x^2 = (x^2 + 3)^2 - 4x^2 = (x^2 + 2x + 3)(x^2 - 2x + 3)$$

$$\therefore k_1 + k_2 = -2 + 2 = 0$$

10. (C)

Let $a = 857$ and $b = 537$.

$$\text{Use } a^3 - b^3 = (a - b)(a^2 + ab + b^2)$$

11. (A)

Since value of square root is always non-negative.

$$x - 1 = 0, y - 2 = 0, z - 3 = 0$$

$$\therefore x = 1, y = 2, z = 3$$

$$\therefore x + y + z = 1 + 2 + 3 = 6$$

12. (C)

$$\begin{aligned} & \frac{(b-a)(\cancel{b+a})(b^2+a^2)}{a(\cancel{a+b})} - \frac{b^3}{a} \\ &= \frac{b^2 - ab + a^2}{b^2 - ab + a^2} \\ &= \frac{1}{a} \left[\cancel{b^3} + a^2b - ab^2 - a^3 - \cancel{b^3} \right] \\ &= \frac{ab - b^2 - a^2}{b^2 - ab + a^2} \\ &= -1 \end{aligned}$$

13. (A)
 $P(1) = 1 + a + b + c = 2 \Rightarrow a + b + c = 1 \quad \dots (1)$
 $P(2) = 8 + 4a + 2b + c = 6 \Rightarrow 4a + 2b + c = -2 \quad \dots (2)$
 $P(3) = 27 + 9a + 3b + c = 12 \Rightarrow 9a + 3b + c = -15 \quad \dots (3)$
 On solving (1), (2) and (3) we get
 $a = -5, b = 12 \text{ and } c = -6$
 $\therefore P(x) = x^3 - 5x^2 + 12x - 6$
 $\therefore P(4) = 4^3 - 5(4)^2 + 12(4) - 6$
 $\therefore P(4) = 26$
14. (D)
 Let $3^{x^2-1} = t$
 $\therefore t^2 - 10t + 9 = 0$
 $\therefore t = 1 \text{ or } t = 9$
 $\therefore 3^{x^2-1} = 1 \text{ or } 3^{x^2-1} = 9$
 $\therefore x^2 - 1 = 0 \text{ or } x^2 - 1 = 2$
 $\therefore x = \pm 1 \text{ or } x = \pm \sqrt{3}$
15. (A)
 Let α be one root of $x^3 + 3x + 2k = 0$
 $\therefore x^2 + 3x + 2k = (x - \alpha)(x - 2\alpha) = x^2 - 3\alpha x + 2\alpha^2$
 $\therefore 3 = -3\alpha \text{ and } 2k = 2\alpha^2$
 $\therefore \alpha = -1 \text{ and } \alpha^2 = k$
 $\therefore k = 1$
 $k = 1$ satisfy $x^2 - 2x + 1 = 0$
16. (C)
 For no solution,
 $\frac{3}{p} = \frac{p}{3} \Rightarrow p^2 = 9 \Rightarrow p = \pm 3$
17. (D)
 $b^2x - a^2y + a^2b + ab^2 = 0 \quad \dots (1)$
 $bx - ay + 2ab = 0 \quad \dots (2)$
 By $(1) - (2) \times b$, we get
 $-a^2y + aby + a^2b - ab^2 = 0$
 $\therefore ay(-a + b) = ab(b - a)$
 $\therefore ay = ab$
 $\therefore y = b$
 By putting $y = b$ in equation (2), we get $x = -a$.
 $\therefore (x, y) = (-a, b)$.

18. (B)

Clearly $x = \frac{1}{1+x}$

$$\therefore x^2 + x - 1 = 0$$

$$\therefore x = \frac{-1 \pm \sqrt{1^2 - 4(1)(-1)}}{2}$$

$$\therefore \text{Since } x > 0, x = \frac{-1 + \sqrt{5}}{2}$$

19. (D)

Non-real roots,

$$D < 0$$

$$\therefore (3p)^2 - 4(1)(4) < 0$$

$$\therefore 9p^2 < 16$$

$$\therefore p^2 < \frac{16}{9}$$

$$\therefore -\frac{4}{3} < p < \frac{4}{3}$$

20. (D)

Let x and y be length and breadth of rectangle.

$$\therefore 2(x+y) = 14 \text{ and } xy = 12$$

$$\therefore x = 4 \text{ and } y = 3 \text{ or } x = 3 \text{ and } y = 4$$

$$\begin{aligned} \text{Length of diagonal} &= \sqrt{x^2 + y^2} \\ &= \sqrt{3^2 + 4^2} \\ &= 5 \text{ m} \end{aligned}$$

Section – B

21. (C)

$$\text{Let } (3+2\sqrt{2})^{x^2-7} = t$$

$$\therefore 3-2\sqrt{2} = \frac{1}{3+2\sqrt{2}}$$

$$\text{We get, } t + \frac{1}{t} = 6$$

$$\therefore t^2 - 6t + 1 = 0$$

$$\therefore t = \frac{6 \pm \sqrt{36-4}}{2} = \frac{6 \pm \sqrt{32}}{2} = 3 \pm 2\sqrt{2}$$

$$\therefore (3+2\sqrt{2})^{x^2-7} = 3+2\sqrt{2} \text{ or } (3+2\sqrt{2})^{x^2-7} = 3-2\sqrt{2}$$

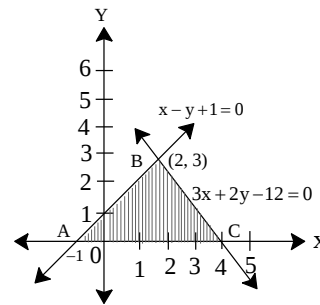
$$\therefore x^2 - 7 = 1 \quad \text{or} \quad x^2 - 7 = -1$$

$$\therefore x^2 = 8 \quad \text{or} \quad x^2 = 6$$

$$\therefore x = \pm\sqrt{8} \quad \text{or} \quad x = \pm\sqrt{6}$$

$$\therefore \text{Sum of square of roots} = 8+8+6+6 = 28$$

22. (A)
From Diagram,
In $\triangle ABC$, length of base is 5 and height is 3.
 $\therefore$ Area of $\triangle ABC = \frac{1}{2} \times 3 \times 5 = \frac{15}{2}$ sq.units.



23. (A)
 $\alpha + \beta = p - 2$ and $\alpha\beta = p^2 + 1$
Also, $(\alpha + \beta)^2 - 2\alpha\beta = \alpha\beta$
 $\therefore (\alpha + \beta)^2 = 3\alpha\beta$
 $\therefore (p - 2)^2 = 3(p^2 + 1)$
 $\therefore p^2 - 4p + 4 = 3p^2 + 3$
 $\therefore 2p^2 + 4p - 1 = 0$
 $\therefore$ sum of all values of p is $-4 / 2 = -2$.

24. (C)
Let the required number be $10x + y$.
From given information,
 $10x + y = 4(x + y)$ and $10x + y = 2xy$
On solving, we get $x = 3$ and $y = 6$
 $\therefore$ The number is 36.

25. (D)
Let the speed of train be x km/hr and car be y km/hr respectively.
According to problem,
 $\frac{280}{x} + \frac{200}{y} = 8$ And $\frac{140}{x} + \frac{340}{y} = \frac{88}{10} = \frac{44}{5}$
On solving we get, $x = 70$ km/hr and $y = 50$ km/hr

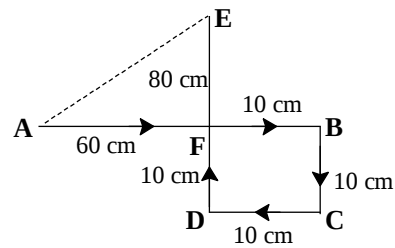
Section – C

26. (B)
Saturday's tomorrow is Sunday. This is my yesterday.
Wednesday's yesterday is Tuesday. This is my tomorrow.
Therefore, today is my Monday.
27. (A)
Q and P are both north of the swing.
But only P is south-west of the slide.
28. (D)
 $3 \times 3 \times 3$ are non-painted small identical cubes.

29. (C)

The movement of Rahul from A to E are as shown in figure.

$$\begin{aligned}
 AE &= \sqrt{(AF)^2 + (FE)^2} \\
 &= \sqrt{60^2 + 80^2} \\
 &= 100
 \end{aligned}$$



30. (D)

A	L	L	O	W	A	N	C	E
-1↓	+1↓	-1↓	+1↓	-1↓	+1↓	-1↓	+1↓	-1↓
Z	N	K	P	V	B	M	D	D
D	E	A	R	N	E	S	S	
-1↓	+1↓	-1↓	+1↓	-1↓	+1↓	-1↓	+1↓	
C	F	Z	S	M	F	R	T	