

1. Work done in cyclic process = Area under the graph

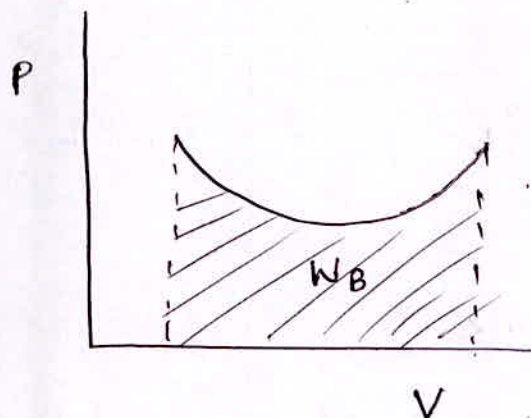
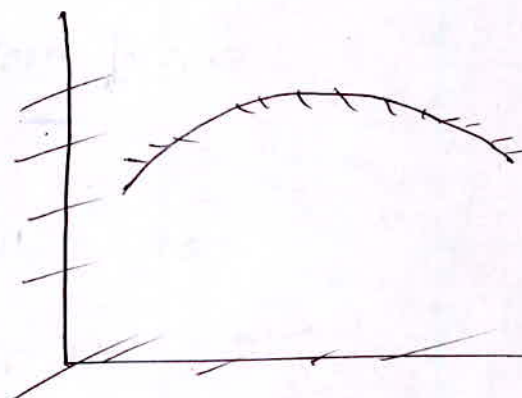
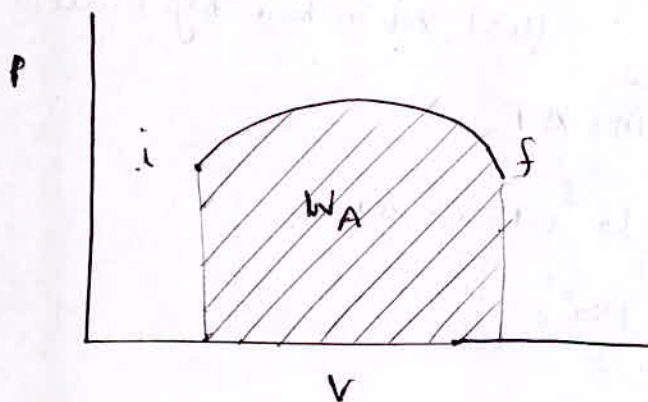
$$\text{Work} = P \times V = PV \quad (+ \text{Work, clockwise})$$

2.  $\Delta Q = \Delta U + \Delta W$

Internal energy is function of state only, so change in internal energy is same but work done in process A is more because <sup>same</sup> volume expansion is done at higher pressure, or you can just see the work by Area under the graph

$$\Delta W = \int_{V_1}^{V_2} P dV$$

$$\Delta Q_A > \Delta Q_B$$



3. Work = Area inside the triangle

$$= \frac{1}{2} \times (P_2 - P_1) \times (V_2 - V_1)$$

$$= 9 P_1 V_1$$

(+) because cycle is clockwise.

4.  $mgh = mc \Delta T$

$$10 \times 100 = \left( \frac{1 \times 4.2}{10^{-3}} \right) \times \Delta T$$

$$\Delta T = \frac{1}{4.2} = 0.23^\circ \text{C}$$

$$(C = 1 \text{ cal/gm}^\circ\text{C})$$

$$= \frac{1 \times 4.2 \text{ Joule}}{10^{-3} \text{ K}}$$

MKS unit

5. Total heat =  $\frac{1}{2} \times 10 \times 10^{-3} \times (300)^2 = \frac{1}{2} mv^2$

$$= 450 \text{ Joule}$$

50% of heat = Heat Absorbed by bullet

$$225 = ms \Delta T$$

$$225 = 10 \times 10^{-3} \times 150 \times \Delta T$$

$$\Delta T = 150^\circ \text{C}$$

6. (B)

7.  $dQ = du + dw$

$$dw = 0$$

$$dQ < 0 \quad \text{so} \quad du < 0$$

So the temperature of ideal gas decreases.

8. a) Isobaric process  $\rightarrow$  constant pressure  $\rightarrow \Delta P = 0$  (3)  
 b) Isochoric process  $\rightarrow$  constant volume  $\rightarrow \int p dv = 0$  ( $dv=0$ )  
 so  $\Delta W = 0$   
 c) Isothermal process  $\rightarrow$  constant T  $\rightarrow \Delta T = 0$   
 d) Isothermal process  $\rightarrow \Delta T = 0 \rightarrow$  so  $du = 0$

Incorrect ✓

$$\text{But } \Delta Q = \Delta U + \Delta W$$

$$\Delta Q = 0 + \Delta W$$

$$\Delta Q = \Delta W$$

10.

Isothermal process

$$pV = \text{constant} = K_1$$

$$p = \frac{K}{V}$$

$$\text{slope of curve} = \frac{dp}{dv} = -\frac{K}{V^2} = -\frac{1}{V} \left( \frac{K}{V} \right) = -\frac{P}{V}$$

Adiabatic process

$$pV^\gamma = \text{constant} = K_2$$

$$p = \frac{K_2}{V^\gamma}$$

$$\left( \frac{dp}{dv} \right) = -\gamma \frac{K_2}{V^{\gamma+1}} = -\frac{\gamma}{V} \left( \frac{K_2}{V^\gamma} \right) = -\gamma \left( \frac{P}{V} \right)$$

$$\frac{\text{slope of Adiabatic process}}{\text{slope of Isothermal process}} = \gamma$$

9. (Bulk Modulus) =  $\frac{P}{\text{Isothermal}}$

(11) ✓ a)  $\Delta Q = \Delta U + \Delta W$

In Adiabatic process

$\Delta Q = 0$

$\Delta U = -\Delta W$

change in internal energy = work done on the system

b) Isothermal process

$\Delta U = 0$

$\Delta Q = \Delta W$

c) Isochoric process

$\Delta W = 0$

$\Delta Q = \Delta U$

(12)  $PV^{\gamma} = \text{constant}$  - (Adiabatic process)

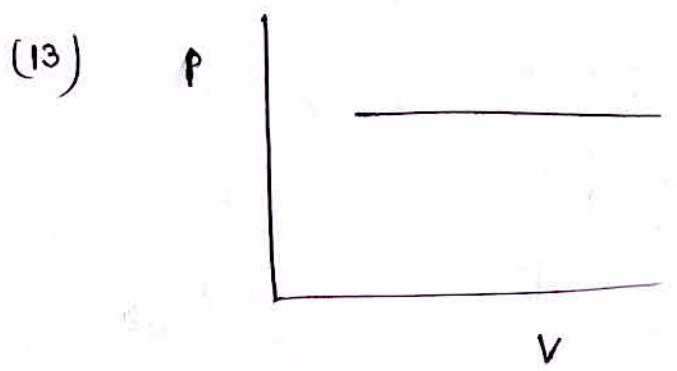
$P_1 V_1^{\gamma} = P_2 V_2^{\gamma}$        $V_2 = \frac{V_1}{8}$

$P_1 V_1^{\gamma} = P_2 \left(\frac{V_1}{8}\right)^{\gamma}$

$P_2 = P_1 (8)^{\gamma}$

$= P_1 \times (2^3)^{\frac{5}{2}}$

$= 32 P_1$



constant pressure

Isobaric process

(14)

Isobaric process

(5)

$$Q = n C_p \Delta T$$

$$\Delta U = n C_v \Delta T$$

$$W = Q - \Delta U$$

$$= n (C_p - C_v) \Delta T$$

$$= n R \Delta T$$

$$= \left(\frac{1000}{2}\right) \times \left(\frac{8.31}{4.2}\right) \times (20 - 10)$$

$$= 500 \times 2 \times 10$$

$$= 10^4 \text{ calories}$$

(15)

$$W = P (V_2 - V_1)$$

$$= 1.02 \times (3.34 - 2 \times 10^{-3}) \times 10^5$$

$$= 340 \text{ KJ}$$

(16)

$$\Delta Q = \Delta U + \Delta W$$

$$\Delta U = 0, \text{ same state}$$

$$\Delta Q = \Delta W = \text{Area of circle}$$

$$= \pi R^2$$

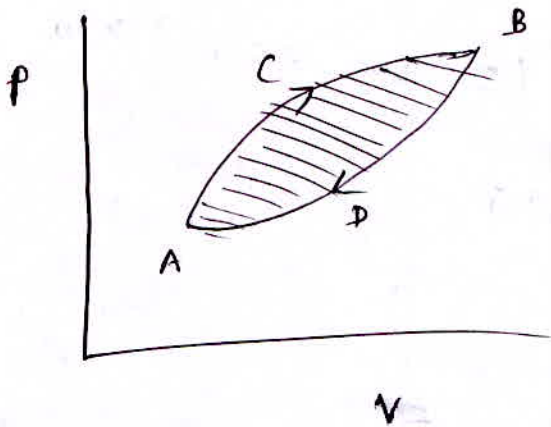
$$= \pi (10 \times 10^3)^2 \text{ kPa-litre}$$

$$= 10^9 \pi \text{ kPa-litre}$$

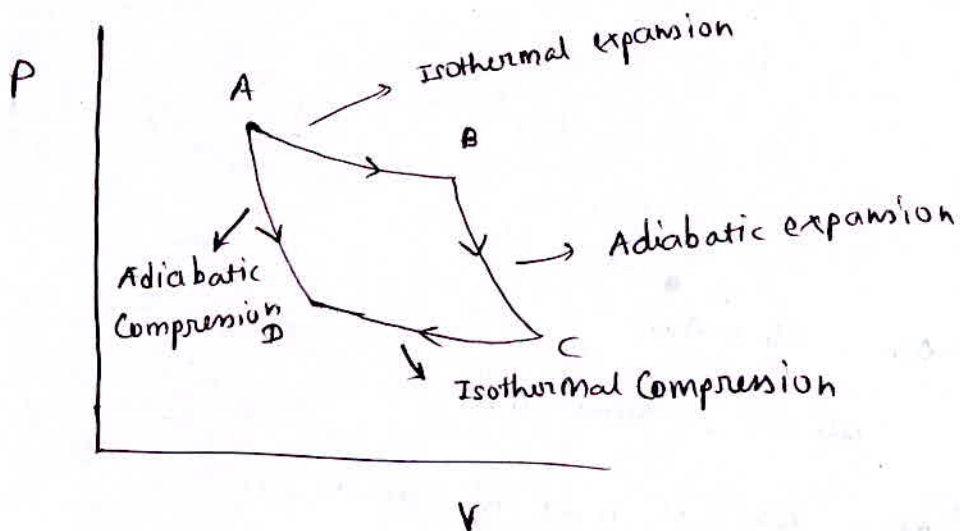
$$\begin{aligned}
 &= \pi 10^3 \text{ kPa-litre} \\
 &= \pi 10^9 \text{ kPa} \cdot \left(\frac{1}{1000}\right) \text{ m}^3 \\
 &= \pi \times 10^2 \times 10^3 \times \frac{1}{1000} \text{ p-m}^3 \\
 &= \pi \times 10^2 \left(\frac{\text{N} \cdot \text{m}^3}{\text{m}^2}\right) \\
 &= \pi \times 10^2 \text{ joule}
 \end{aligned}$$

(17) (D)

(18) Net work done = Area inside the curve  
= ACBDA



(19)



(20) (D)

1.

$$\begin{aligned} \text{WORK} &= \text{Area Inside cycle} \\ &= \frac{1}{2} \times 2P_1 \times 2V_1 \\ &= 2P_1 V_1 \end{aligned}$$

2.

$$\Delta Q = \Delta U + \Delta W$$

a) Not necessary, if the process is isothermal, then all the heat will be used in work done, so  $\Delta U$  can be zero

b) Internal energy is a function of temperature

$$\Delta U = nC_V \Delta T$$

always increase with increase in temperature

c)  $\Delta Q = \Delta U + \Delta W$

$$0 = \Delta U + \Delta W$$

$$\Delta U = -\Delta W$$

If  $\Delta W$  is negative that is work is done on the system then  $\Delta U$  will increase

d)  $\square$  does not depend on velocity of vessel

3.

$$W_{AB} = P(V_2 - V_1) = P_0 (V_0 - 2V_0) = -P_0 V_0$$

$$W_{BC} = \int P dv = 0 \quad (dv=0)$$

$$W_{CD} = P \int_{V_0}^{3V_0} P dv = P \int_{V_0}^{3V_0} dv \quad [P \text{ constant}]$$

$$= 2P_0 (3V_0 - V_0) = 4P_0 V_0$$

$$W_{ABCD} = -P_0 V_0 + 0 + 4P_0 V_0 = 3P_0 V_0$$

4. 50% of Energy =  $ms \Delta T$

$$\frac{1}{2} \times \left( \frac{1}{2} m v^2 \right) = m \times s \times \Delta T$$

$$\Delta T = \frac{v^2}{4s}$$

5.  $mg(h_2 - h_1) = ms \Delta T$

$$\frac{9.8 \times 24.5}{252} = \Delta T$$

$$\Delta T = 0.95 \text{ K}$$

6.  $Q = mc \Delta T$

$$4200 \text{ Joules} = m \times \left( \frac{4.2}{4.2} \right) \Delta T = m \times 4.2 \times \Delta T$$

$$m \Delta T = 1000 \quad (m \text{ in gm})$$

7.  $\Delta Q = \Delta U + \Delta W$

$$200 = \Delta U + (-100)$$

$$\Delta U = 300 \text{ J}$$

[W is Negative because work is done on the system]

8.  $\Delta Q = \Delta U + \Delta W$

$$-20 = \Delta U + (-8)$$

$$\Delta U = -20 + 8 = -12$$

$$U_f - U_i = -12$$

$$U_f = 30 - 12$$

$$= 18 \text{ J}$$



9.  $Q = n c_p \Delta T$   
 $= n c_p (T_2 - T_1)$

$dw = p dv$   
 $w = \int_{v_1}^{v_2} p dv$   
 $= p \int_{v_1}^{v_2} dv$  (pressure constant)  
 $= p (v_2 - v_1)$

10. a) At equilibrium pressure on both side will be equal

pressure =  $\frac{\text{Force Applied by spring at equilibrium}}{\text{Area}}$   
 $= \frac{k x_0}{s}$

b) work done by the gas  
 $= \int p dv$   
 $= \int_0^{x_0} \left(\frac{kx}{s}\right) \times (s dx)$   
 $= \int_0^{x_0} kx dx$   
 $= k \left(\frac{x_0^2}{2}\right)$

c)  $\Delta Q = du + \Delta w$   
 chamber is thermally insulated  
 so  $\Delta Q = 0$   
 $du = -\Delta w = -\frac{kx_0^2}{2}$

$$(d) \quad du = \frac{-kx_0^2}{2}$$

Internal energy decreased so the temperature will also decrease.

$$du = n c_v \Delta T$$

(ii).

$$\Delta Q = du + \Delta W$$

$$du = 0, \quad \text{Isothermal process} \quad \Delta T = 0$$

$$\Delta Q = \Delta W$$

[work is done on the system]

$$\Delta Q = -1.5 \times 10^4 \text{ J}$$

$$= \frac{-1.5 \times 10^4}{4.2} \text{ calories}$$

$$= -0.36 \times 10^4 \text{ calories}$$

$$= -3.6 \times 10^3 \text{ calories}$$

(A)

$$(12) \quad \text{Initial Energy} = \frac{f}{2} NRT \quad f = 5 \text{ For diatomic gas}$$

$$= \frac{5}{2} NRT$$

$$\text{Final Energy} = \frac{3}{2} \times (2n) RT + \frac{5}{2} (N-n) RT$$

$$= \cancel{3NRT} \quad 3nRT + \frac{5}{2} (N-n) RT$$

$$\text{Heat supplied to the gas} = \cancel{3NRT} - \cancel{\frac{5}{2} NRT}$$

$$= \cancel{\frac{1}{2} NRT}$$

$$= 3nRT + \frac{5}{2} (N-n) RT - \frac{5}{2} NRT$$

$$= 3nRT - \frac{5}{2} nRT = \frac{1}{2} nRT$$

13.  $\Delta Q = dU + \Delta W$

$0 = -100 + \Delta W$

$\Delta W = 100$

14.  $PV^\gamma = K$

$P = +KV^{-\gamma}$

$\frac{\Delta P}{P} = -\gamma \frac{\Delta V}{V}$

$\left[ \begin{aligned} y &= x^n \\ \frac{\Delta y}{y} &= n \frac{\Delta x}{x} \end{aligned} \right]$

15. In adiabatic process

$\Delta Q = dU + \Delta W$

$\Delta W = -\Delta U$

Internal energy of the gas is used in doing work

16. Adiabatic elasticity =  $\frac{dP}{-dV/V} = \gamma P$

=  $1.4 \times 10^5 \text{ N/m}^2$

17. Identical Adiabatic vessels, same volume

$P \propto T$

$dU = nC_v dT$

$U \propto T$

$U \propto P$

$\frac{U_{01}}{U_{02}} = \frac{P_1}{P_2}$

Finally the temperature will be equal

so Internal energy will be equal

$$U_{f_1} = U_{f_2}$$

18. process is Adiabatic.

$$\Delta Q = 0$$

19.

$$\begin{aligned}
 W &= \int P dV \\
 &= P_{\text{atmosphere}} \int_{1 \text{ cm}^3}^{1671 \text{ cm}^3} dV \\
 &= 1.02 \times 10^5 \times 1670 \times (10^{-6}) \text{ N-m} \\
 &= 170.34 \text{ Joule} \\
 &= \frac{170.34}{4.2} \text{ calorie} = 40.55 \text{ cal.}
 \end{aligned}$$

20.

$$\Delta Q = 540 \text{ cal.} = 540 \times 4.2 \text{ J} = 2268 \text{ J}$$

$$\begin{aligned}
 \Delta W &= 1.01 \times 10^5 \times 1670 \times 10^{-6} \\
 &= \underline{168.67} \text{ Joule}
 \end{aligned}$$

$$= \frac{168.67}{4.2} =$$

$$\Delta U = 2268 - 168.67$$

$$= 2099 \text{ J}$$



25 (c)



## Assertion And Reasons

1. It's An Adiabatic process

$$\Delta Q = 0$$

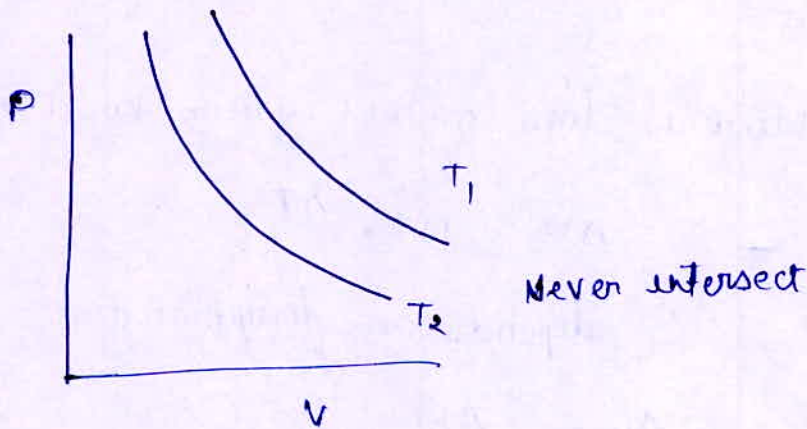
$$\Delta U = -\Delta W \quad (\text{work is positive, expansion})$$

Temperature will decrease

2. In thermodynamic process, entropy will ~~some energy~~ will be ~~wasted in non conservative~~ There will be a heat loss, so irreversible

3. Same as (1)

4.



5. — Not necessary, if volume decrease, work is negative

$$\Delta U = -\Delta W$$
$$= +ve$$

Temp.  $\uparrow$

— Not necessary slow process

6. - All heat converts into work  $\Delta U = 0$

- It's correct

7. - No, we can change it, Adiabatic process

8.  $dQ = m c dT$

9. —

10. No.  $\Delta Q = \Delta U + \Delta W$

Not necessarily

11. - Energy Conservation

- Wrong Higher T  $\rightarrow$  lower T

12. —

13. Work is done on the system, so Temperature increase

14.  $\Delta U = n c_v \Delta T$

depends on temperature

15.  $\Delta U = -\Delta W$

$$TV^{\gamma-1} = K$$

$$T = \frac{K}{V^{\gamma-1}}$$

depends on volume

16.  $ds = \int \frac{dQ}{T}$

$dQ = 0$ , in Adiabatic

$$\text{so } ds = 0$$



17.  $\Delta Q = \Delta U + \Delta W$  Energy Conservation

$$\text{Energy} = M^1 L^2 T^{-2}$$

M, L, T Are fundamental

18. Zeroth law leads to Concept of temperature

19. 
$$\eta = 1 - \frac{T_{\text{sink}}}{T_{\text{source}}}$$

$$\eta = \frac{W}{Q_{\text{in}}}$$

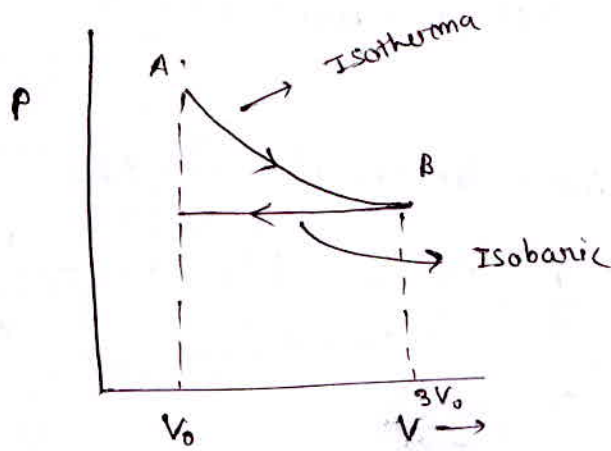
20. - wrong highest for gas

- ~~Atoms are~~ correct





4. (D)



5.

$$\Delta Q = n C_p \Delta T$$

$$310 = 2 \times C_p \times (35 - 25)$$

$$C_p = \frac{310}{20} = 15.5 \text{ J/mol-K}$$

$$C_p = C_v + R$$

$$C_v = C_p - R = 15.5 - 8.31$$

$$C_v = 7.2 \text{ J/mol-K}$$

At constant volume

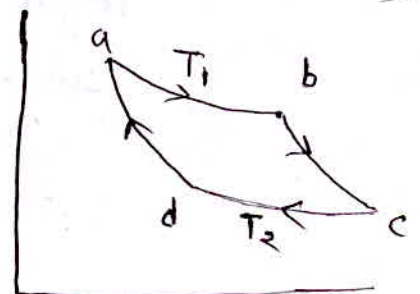
$$\begin{aligned} \Delta Q &= n C_v \Delta T \\ &= 2 \times 7.2 \times 10 \\ &= 144 \text{ Joule} \end{aligned}$$

6.  $W_{ab} + W_{bc} + W_{cd} + W_{da} > 0$  clockwise cycle  
 work done in A to B is more positive than  
 Negative work done from c to D. [Area under the graph]

$$W_{b \rightarrow c} = -W_{d \rightarrow a}$$

$$W_{b \rightarrow c} = -W_{d \rightarrow a}$$

$$W_{b \rightarrow c} + W_{d \rightarrow a} = 0$$



7.

$$ds = \int \frac{dQ}{T}$$

$$= \frac{80 \times 1000}{273}$$

$$= 293 \text{ cal/K}$$

8. a) In process AB and CD, heat is given to the system, but temperature is constant, All the heat is being used in changing the state of material

b) ———

$$c) \quad Q_{AB} = m \times L_f$$

$$Q_{CD} = m \times L_v$$

$$Q_{CD} = 2 Q_{AB}$$

$$m L_v = 2 \times m L_f$$

$$L_v = 2 L_f$$

(Incorrect option)

d) ———

$$e) \quad L_v = 2 L_f$$

9.

$$\text{Temp} \quad \frac{A-72}{110} = \frac{B-72}{220}$$

$$\frac{A-72}{110} = \frac{A-72}{220}$$

$$2A - A = 72^\circ$$

10.

(c)

11.

process is Isochoric (Constant volume)

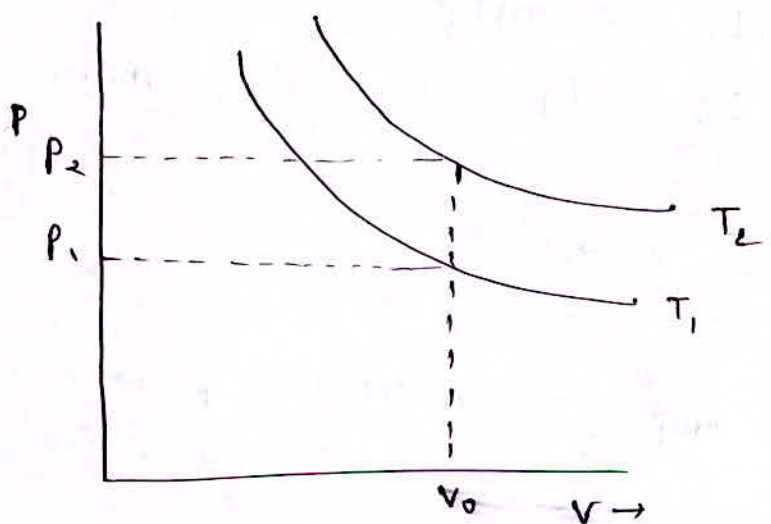
$$\begin{aligned}
 Q &= n C_v \Delta T \\
 &= 2 \times \frac{5}{2} R \times \Delta T \\
 &= 2 \times \frac{3}{2} \times 8.31 \times 20 \\
 &= 498 \text{ J}
 \end{aligned}$$

12.

Isothermal process

$$\begin{aligned}
 W &= nRT \ln \left( \frac{V_2}{V_1} \right) \\
 &= 10 \times 8.31 \times 600 \ln \left( \frac{10}{100} \right) \\
 &= ~~4.4~~ -11.4 \times 10^4 \text{ J}
 \end{aligned}$$

13.



At a volume  $V_0$  for both, pressure is more for  $T_2$  graph.

$P \propto T$  (same volume)

$P_2 > P_1 \rightarrow T_2 > T_1$

14.  $\Delta Q = \Delta U + \Delta W$

$\Delta U$  will be same for both process.

$$8 \times 10^5 = \Delta U + 6.5 \times 10^5$$

$$\Delta U = 1.5 \times 10^5 \text{ J}$$

$$\Delta Q = \Delta U + \Delta W$$

$$10^5 = 1.5 \times 10^5 + \Delta W$$

$$\Delta W = -0.5 \times 10^5 \text{ J}$$

$0.5 \times 10^5 \text{ J}$  work is done on the gas.

15.  $W = nRT \ln \left( \frac{V_2}{V_1} \right)$

$$= RT \ln \left( \frac{V_2}{V_1} \right)$$

16. (c)

17. (d)

18. Work = Area under the graph

$$\Delta U = 0 \quad (\text{same state})$$

$$Q = \Delta U + W = 0 + W = W$$

19. Initial energy = Final energy

$$\frac{5}{2} \times 1 \times R T_0 + \frac{3}{2} \times 1 \times R \times \frac{7T_0}{3} = \frac{5}{2} R T_f + \frac{3}{2} R T_f$$

$$6RT_0 = 4RT_f$$

$$T_f = \frac{3}{2} T_0$$

20.  $\Delta Q = \Delta U + \Delta W$

$\Delta U = 0$  (cyclic process)

$$Q_1 + Q_2 + Q_3 + Q_4 = W_1 + W_2 + W_3 + W_4$$

$$W_4 = 765 \text{ J}$$

21. No diagram

22. (c)

23. At constant pressure

$$\Delta Q = n C_p \Delta T$$

$$\Delta U = n C_v \Delta T$$

$$\Delta W = n C_p \Delta T - n C_v \Delta T$$

$$\text{Fraction} = \frac{n C_p \Delta T - n C_v \Delta T}{n C_p \Delta T}$$

$$= 1 - \frac{1}{\gamma}$$

24.  $\Delta W = P (V_2 - V_1)$  Isobaric

$$= 50 (4 - 10)$$

$$= -300 \text{ J}$$

$$\Delta Q = \Delta U + \Delta W$$

$$100 = \Delta U - 300$$

$$\Delta U = 400 \text{ J}$$



25. (A) Not necessary, In isothermal process temperature remains constant. All the heat given to the system is used in work.

(B)  $W = \int_{V_1}^{V_2} P dv$

If  $W$  is positive then volume will always increase

26. ~~At~~ Some heat is used to do work and some heat is used to overcome intermolecular forces and becomes its internal energy.

$$\Delta Q = \Delta U + \Delta W$$

$$540 \times 4.19 \text{ J} = \Delta U + 1.013 \times 10^5 \times (1.671 - 1) \times (10^{-6} \text{ m}^3)$$

$$\Delta U = 500 \quad 2023.429 \text{ Joule}$$

$$= 500 \text{ caloric}$$

27. a) doesn't change in isothermal or cyclic process.

b) depends only on state, Both internal energy and Entropy

c) Isoentropic process

d)  $\Delta Q = 0, \quad \Delta W = -\Delta U$

28. volume decreases (Ice  $\rightarrow$  Water at  $0^\circ$ )

29. cyclic process,  $\Delta U = 0$

$$\Delta Q = \Delta U + \Delta W$$

$$\Delta Q = \Delta W$$

$$\Delta Q_{A \rightarrow B} + \Delta Q_{B \rightarrow C} + \Delta Q_{C \rightarrow A} = \Delta W_{A \rightarrow B} + \Delta W_{B \rightarrow C} + \Delta W_{C \rightarrow A}$$

$$5 = P(V_2 - V_1) + 0 + W_{C \rightarrow A}$$

Isobaric      Isobaric

$$5 = 10 \times 1 + W_{C \rightarrow A}$$

$$W_{C \rightarrow A} = -5 \text{ J}$$

30. Work done by conservative force depends on the path.

$$31. \quad \Delta Q = \Delta U + \Delta W$$

$$150 = \Delta U + 110$$

$$\Delta U = 40 \text{ J}$$

$$32. \quad Q_1 + Q_2 + Q_3 + Q_4 = W_1 + W_2 + W_3 + W_4$$

$$X = 1000 - 300 = 700 \text{ J}$$

$$\eta = \frac{1000 \times 100}{9500} = 10.5 \%$$

33.

$$W = \int P dv$$

$$= 0$$

$$(dv = 0)$$

34.

a) Internal energy depends only on the state, function of temperature

b) Isothermal process  $\Delta T = 0$ ,  $\Delta U = n c_v \Delta T = 0$

c) Area under p-v graph is work

d) ~~W~~ Work and heat, both are path dependent.

35.

(a)

36.

$$\text{Work} = \text{Area}$$

$$= (+) P \times V$$

( $\dot{=}$  clockwise cycle)

37.

$$W = \frac{1}{2} \times 2V \times P = PV$$

38.

$$\Delta Q = \Delta U + \Delta W$$

$$-30 = \Delta U - 10$$

$$\Delta U = -20$$

$$U_f - U_i = -20$$

$$U_f = 40 - 20 = 20 \text{ J}$$

39.  $\Delta Q = \Delta U + \Delta W$

$\Delta U = \Delta Q - \Delta W$  (Not a path function)

40.  $\Delta Q = \Delta U + \Delta W$

$40 = \Delta U + 30$

$\Delta U = 10 \text{ J}$

41. Question from Assertion and Reason

Q.2

42.

Isobaric process

$$W = P(V_2 - V_1)$$

$$= 2 \times 10^5 \times (150 - 50) \times 10^{-3}$$

$$= 2 \times 10^4 \text{ J}$$

$$1 \text{ litre} = 1000 \text{ mL}$$

$$= 1000 \text{ cm}^3$$

$$= 1000 \times 10^{-6} \text{ m}^3$$

$$= 10^{-3} \text{ m}^3$$

43.

$$= 200 \times 4.19 \text{ Joule}$$

$$= 838 \text{ joule}$$

44

(c)

45. When temperature of gas increase, its internal energy always increase.

$$\Delta Q = \Delta U + \Delta W$$

Temperature can also increase if no heat is given to the system

$$\Delta Q = 0 = \Delta U + \Delta W$$

$$\Delta U = -\Delta W$$

(if  $\Delta W$  is negative, then  $\Delta U \uparrow, T \uparrow$ )

47. Temperature can also increase, if no work is done by the gas, All the heat supplied to the gas goes into internal energy, process is isochoric.

$$\Delta Q = \Delta U + \Delta W =$$

$$= \Delta U + 0$$

$$= \Delta U$$

$$\Delta Q \uparrow \rightarrow \Delta U \uparrow \rightarrow T \uparrow$$

47. (d)

48.  $W = \text{Area of Rectangle}$  (+ because clockwise)

$$= 2p \times 2v$$

$$= 4pV$$

49.

$$\Delta Q = \Delta U + \Delta W$$

$$110 = 40 + \Delta W$$

$$\Delta W = 70 \text{ J}$$

50.

Work = Area of Triangle (+ve, clockwise)

$$= \frac{1}{2} \times 2 \text{ V} \times 3 \text{ P}$$

$$= 3 \text{ PV}$$

## Thermodynamic processes

1.  $C_p' - C_v' = R$ , When  $C_p'$  and  $C_v'$  are molar heat capacity

$$C_p' - C_v' = R$$

For Nitrogen  $28 C_p - 28 C_v = R$   
 $28 (C_p - C_v) = R$   
 $28 (m) = R$   
 $m = \frac{R}{28}$

For Hydrogen  $C_p' - C_v' = R$   
 $2 C_p - 2 C_v = R$   
 $C_p - C_v = \frac{R}{2}$   
 $m = \frac{R}{2}$

$$28m = 2m$$

$$14m = m$$

2.  $\eta = 1 - \frac{T_2}{T_1} = 1 - \left( \frac{127 + 273}{227 + 273} \right)$   
 $= 1 - \frac{400}{500} = 0.2 \Rightarrow 20\%$

$$\eta = \frac{\text{Work done}}{\text{Heat Input}} = 0.2$$

$$\text{Work done} = 0.2 \times 6 \times 10^4$$
$$= 1.2 \times 10^4 \text{ J}$$

3. (b)

4.  $\Delta Q = 0$

$$\Delta Q = \Delta W + \Delta U$$

$$\Delta U = -\Delta W \begin{matrix} \searrow \text{positive} \\ \text{= Negative} \end{matrix}$$

Temperature will decrease

~~$$PV = nRT$$~~

~~$$P = \frac{nRT}{V}$$~~

$$PV^\gamma = K$$

$$P = \frac{K}{V^\gamma}$$

$$V \uparrow \quad P \downarrow$$

5.

$$pV^\gamma = \text{constant}$$

$$P_1 V_1^\gamma = P_2 V_2^\gamma$$

$$\frac{P_2}{P_1} = \left(\frac{V_1}{V_2}\right)^\gamma = \left(\frac{V_1}{V_1/8}\right)^{\frac{5}{3}} = (2^3)^{\frac{5}{3}} = 32$$

6.

Question from Assertion Reason

Q.4

8.

$$pV^\gamma = K$$

$$P = KV^{-\gamma}$$

$$\frac{\Delta P}{P} = -\gamma \frac{\Delta V}{V} \quad \Rightarrow \quad \frac{\Delta V}{V} = -\frac{2}{3} \times \frac{3}{3} = -\frac{4}{9}\%$$



$$7. W_{\text{Adiabatic}} = \frac{nR(T_i - T_f)}{\gamma - 1} = \bullet$$

$$-146 \times 10^3 = \frac{1000 \times 8.314 \times (-\cancel{7})}{\gamma - 1}$$

$$\gamma - 1 = \cancel{0.45} 0.397$$

$$\gamma = 1.45 = 1 + \frac{2}{f}$$

$$\gamma = 1.397 \approx 1.4$$

$$f = \frac{2}{0.45}$$

Diatomic

$$f =$$

9.

$$PV^\gamma = K$$

$$\frac{nRT}{V} V^\gamma = K$$

$$TV^{\gamma-1} = K_1$$

10.

$$TV^{\gamma-1} = K$$

$$T = \frac{K}{V^{\gamma-1}}$$

Adiabatic  
expansion

$$V \uparrow, T \downarrow$$

11.

Isothermal

12. (c)  $dp = 0$

$$= -\frac{dp}{\frac{dv}{v}}$$

13.  $PV^\gamma = K$

$$P \left( \frac{nRT}{P} \right)^\gamma = K$$

$$P^{1-\gamma} T^\gamma = K \frac{1}{1-\gamma}$$
$$P = \left( \frac{K}{T^\gamma} \right)^{\frac{1}{1-\gamma}} = T^{\frac{1}{\gamma(Y-1)}} \times K^{1-\gamma}$$

$$\frac{Y}{Y-1} = 3 \Rightarrow Y = 3Y - 3$$
$$\frac{C_p}{C_v} = Y = \frac{3}{2} = 1 + \frac{2}{f}$$

14. Isothermal process  $\Delta T = 0$

$$dU = nC_v \Delta T$$

Increase  $\eta$

15. —

16. Adiabatic  $\Delta Q = 0 = \Delta U + \Delta W$

$$\Delta U = -\Delta W$$

Isothermal  $\Delta U = 0$

17.

$$PV^\gamma = K$$

$$P \left( \frac{nRT}{P} \right)^\gamma = K$$

$$P^{1-\gamma} T^\gamma = K_1$$

$$P = K_1 T^{\frac{\gamma}{\gamma-1}}$$

$$C = \frac{\gamma}{\gamma-1} = \frac{5/3}{2/3} = \frac{5}{2}$$

$$\left[ \begin{aligned} \gamma &= 1 + \frac{2}{f} \\ &= 1 + \frac{2}{3} \\ &= \frac{5}{3} \end{aligned} \right.$$

monatomic

18.

Adiabatic process

$$PV^\gamma = K$$

$$P \left( \frac{nRT}{P} \right)^\gamma = K$$

$$P^{1-\gamma} T^\gamma = K_1$$

$$T = K_1^{1/\gamma} (P)^{-1/\gamma}$$

$$\frac{T_2}{T_1} = \left( \frac{1}{8} \right)^{2/3} = [8]^{-2/3}$$

19.

Thermos flask  $\Delta Q = 0$ ~~Work is done by the system~~

Mechanical energy given to the system is converted into heat

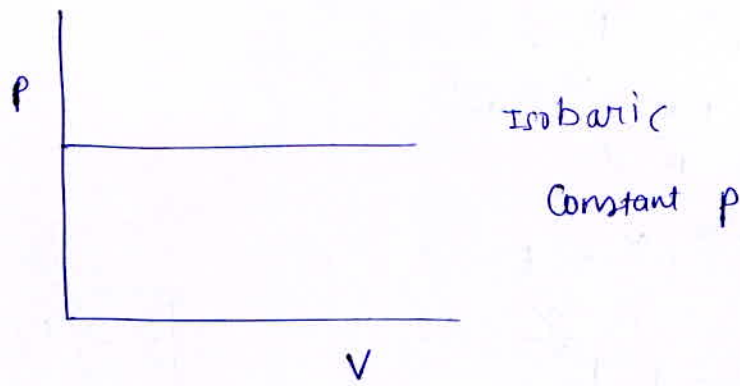
20.

$$PV^\gamma = K$$

$$\frac{nRT}{V} (V^\gamma) = K$$

$$TV^{1-\gamma} = K_1$$

21.



22.

$$ds = \int \frac{dq}{T}$$

Temperature Constant

$$ds = \frac{1}{T} \int dq$$

$$dq = du + dw$$

$$dq = 0 + dw = dw$$

$$ds = \frac{1}{T} \int dw = \frac{1}{T} \times nRT \ln \frac{V_2}{V_1}$$

$$= nR \ln \frac{V_2}{V_1}$$

23.

$$W_{\text{Isothermal}} = nRT \ln \left( \frac{V_2}{V_1} \right)$$

$$= nRT \ln \left( \frac{V_2}{V_1} \right)$$

24.

$$\text{Isochoric} \rightarrow dv = 0$$

$$\Delta Q = \Delta U + \Delta W$$

$$\Delta Q = \Delta U$$

25.

It's Adiabatic expansion

$$PV^\gamma = K$$

~~$$\frac{nRT}{V} \times V^\gamma = K$$~~

$$TV^{\gamma-1} = K_1$$

$$T = \frac{K_1}{V^{\gamma-1}}$$

$V \uparrow$ , so  $T \downarrow$

26.

$$PV^{3/2} = K$$

$$\frac{nRT}{V} \times V^{3/2} = K$$

$$T\sqrt{V} = K_1$$

$$\frac{T_2}{T_1} = \sqrt{\frac{V_1}{V_2}} = \sqrt{2}$$

$$T_2 = \sqrt{2} T_1$$

27.

$$P_1 V_1^\gamma = P_2 V_2^\gamma$$

$$P_1^{1-\gamma} T_1^\gamma = P_2^{1-\gamma} T_2^\gamma$$

$$\left(\frac{T_2}{T_1}\right)^\gamma = \left(\frac{P_2}{P_1}\right)^{\gamma-1}$$

$$T_2 = T_1 \times \left(\frac{P_2}{P_1}\right)^{\frac{\gamma-1}{\gamma}}$$

~~⊗~~

28.

$$W = \frac{nR(T_i - T_f)}{\gamma - 1} = 6R$$

$$T_i - T_f = 6(\gamma - 1)$$

$$T_i - T_f = 6\left(\frac{5}{3} - 1\right)$$

$$T_i - T_f = 10 - 6 = 4$$

$$T_f = T_i - 4 = T - 4$$

29.

(c)

30.

$$\begin{aligned} \Delta W &= P(V_2 - V_1) \\ &= 50(4 - 10) \\ &= -300 \text{ J} \end{aligned}$$

$$\Delta Q = \Delta U + \Delta W$$

$$100 = \Delta U - 300$$

$$\Delta U = 400 \text{ J}$$

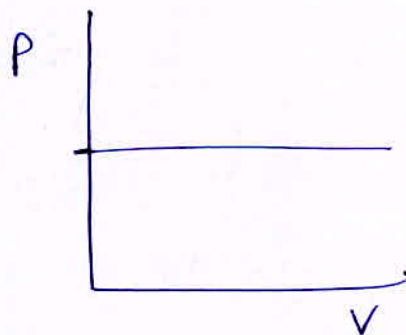
31.

(B)

32.

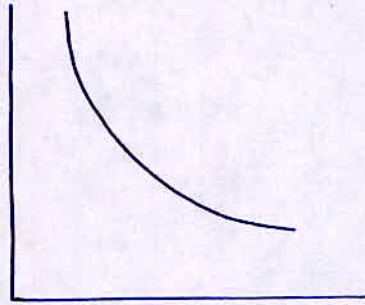
constant  $V$ 

$$P \propto T$$



33. (A) Atmospheric pressure

34.  $p \propto \frac{1}{V}$



35. - Adiabatic process

$$pV^\gamma = K$$

$$\frac{P_2}{P_1} = \left(\frac{V_1}{V_2}\right)^\gamma = \left(\frac{V}{2V}\right)^{\frac{3}{2}} = \frac{1}{2\sqrt{2}}$$

$$P_2 = \frac{1}{2\sqrt{2}} \times 2\sqrt{2} P = P$$

- Isobaric process

$$P_1 = P_2 = P$$

- Isothermal process

$$\frac{P_2}{P_1} = \frac{V_1}{V_2} = \frac{1}{2}$$

$$P_2 = \frac{2P}{2} = P$$

$$P : P : P = 1 : 1 : 1$$

36

$$\Delta Q = \Delta U + \Delta W$$

$$\begin{aligned} \text{At constant } P, \quad \Delta Q &= nC_p \Delta T \\ &= n(\gamma C_v) \Delta T \\ &= \gamma (nC_v \Delta T) \\ &= \gamma \Delta U \end{aligned}$$

$$\gamma \Delta U = \Delta U + P(2V - V)$$

$$(\gamma - 1) \Delta U = PV$$

$$\Delta U = \frac{PV}{\gamma - 1}$$

37.

$$T \propto \frac{1}{\sqrt{V}}$$

$$T = \frac{k}{\sqrt{V}}$$

$$TV^{1/2} = k$$

$$\gamma - 1 = \frac{1}{2}$$

$$\gamma = \frac{3}{2}$$

38.

$$PV = nRT$$

~~PV~~, constant pressure

$$V \propto T$$

$$T_1 = 300$$

$$T_2 = 600$$

$$PV_2 = nRT_2$$

$$PV_1 = nRT_1$$

$$W = P(V_2 - V_1) = 0.1 \times R (T_2 - T_1)$$

$$= 0.1 \times 2 \times 300$$

$$= 60 \text{ cal.}$$



## Second Law of Thermodynamics

1. 
$$\eta = 1 - \frac{T_2}{T_1} = 1 - \frac{27 + 273}{127 + 273}$$
$$= 1 - \frac{300}{400} = \frac{1}{4}$$

$$\frac{\text{Work done by Engine}}{\text{Heat supplied}} = \frac{1}{4}$$

$$\text{Work done} = \frac{1}{4} \times 40 = 10 \text{ kJ}$$

2. 
$$1 - \frac{T_2}{T_1} = \frac{1}{4} = \frac{25}{100}$$

$$\frac{T_2}{T_1} = \frac{3}{4}$$

$$T_1 = \frac{4}{3} T_2 = \frac{4}{3} \times 300 = 400 \text{ K}$$
$$= (400 - 273)^\circ \text{C}$$
$$= 127^\circ \text{C}$$

3. 
$$\eta = 1 - \frac{T_2}{T_1}$$

$$\frac{1}{4} = 1 - \frac{T - 80}{T}$$

$$\frac{1}{4} = 1 - 1 + \frac{80}{T}$$

$$T = 320 \text{ K}$$

$$= 320 - 273$$

$$T = 47^\circ \text{C}$$

$$\text{Temperature of sink} = T - 80 = 47 - 80 = -33^\circ \text{C}$$

4. (S1)

can't be 1

$$\eta = 1 - \frac{T_2}{T_1}$$

$$T_2 \neq 0$$

(S2)

$$\Delta Q = \Delta U + \Delta W$$

Correct

(S3)

correct

(S4)

~~correct~~

5.

a) doesn't change in isothermal

b) ~~correct~~ correct

(c)  $\Delta S$  - can be zero.

(d)  $\Delta Q = \Delta U + \Delta W$

$$\Delta W = -\Delta U$$

6.

At normal temperature

$$C_V = \frac{f}{2} R$$

$$C_V = \frac{3}{2} R$$

$f = 3$  For monoatomic

at very high temperature

$$C_V = \frac{5}{2} R$$

$f = 5$  For monoatomic

No vibration

No rotation

For diatomic  $\rightarrow$

At Normal Temperature

$$f = 5 \quad (3 \text{ translational} + 2 \text{ rotational})$$

$$C_V = \frac{5}{2} R$$

At higher temperature

$$f = 7$$

$$C_V = \frac{7}{2} R$$

8.

$$\eta = 1 - \frac{T_2}{T_1}$$

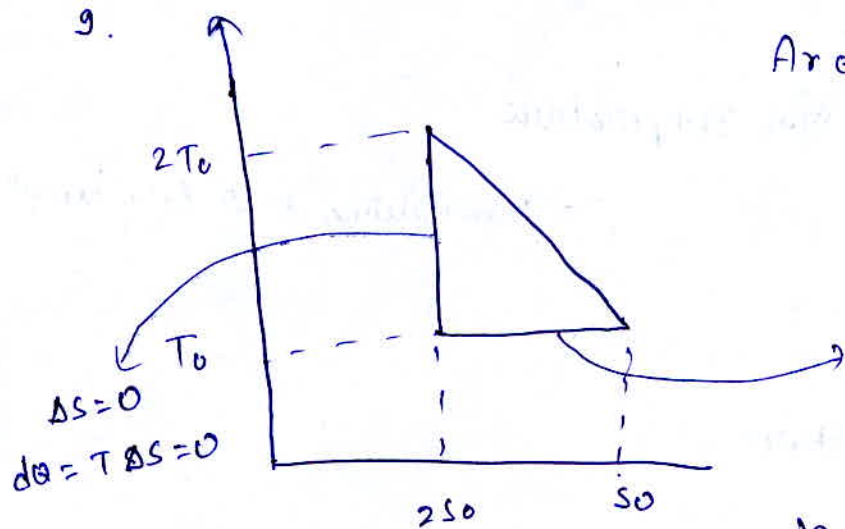
$$= 1 - \frac{27 + 273}{627 + 273}$$

$$= 1 - \frac{300}{900}$$

$$= \frac{2}{3}$$

7.

9.



$$\begin{aligned} \text{Area of cyclic process} &= Q_{in} - Q_{out} \\ &= W \\ Q_{in} - Q_{out} &= \frac{1}{2} T_0 S_0 \end{aligned}$$

$$\begin{aligned} dQ &= T dS \\ Q_{out} &= T_0 S_0 \\ n &= \frac{Q_{in} - Q_{out}}{Q_{in}} \\ &= \frac{\frac{1}{2} T_0 S_0}{\frac{1}{2} T_0 S_0 + T_0 S_0} = \frac{1}{3} \end{aligned}$$

10. —

$$11. \quad \eta = 1 - \frac{T_2}{T_1}$$

$$\frac{1}{2} = 1 - \frac{300}{T_1}$$

$$T_1 =$$

$$\frac{2}{5} = 1 - \frac{300}{T_1}$$

$$\frac{300}{T_1} = \frac{3}{5}$$

$$T_1 = 500 \text{ K}$$

$$\frac{60}{100} = 1 - \frac{300}{T_1'}$$

$$\frac{300}{T_1'} = \frac{4}{10} = \frac{2}{5}$$

$$T_1' = 600 \text{ K} \quad 750 \text{ K}$$

$$T_1' - T_1 = 250 \text{ K}$$

12.

$$\frac{1}{2} = 1 - \frac{273 + 50}{T_1}$$

$$\frac{323}{T_1} = \frac{1}{2}$$

$$\begin{aligned} T_1 &= 646 \text{ K} \\ &= 646 - 273 \\ &= 373^\circ \text{C} \end{aligned}$$

13.

$$\frac{1}{6} = 1 - \frac{T_2}{T_1}$$

$$\frac{T_2}{T_1} = \frac{5}{6}$$

$$\frac{1}{3} = 1 - \frac{T_2 - 62}{T_1}$$

$$\frac{T_2 - 62}{T_1} = \frac{2}{3}$$

$$\frac{T_2}{T_1} - \frac{62}{T_1} = \frac{2}{3}$$

$$\frac{5}{6} - \frac{2}{3} = \frac{62}{T_1}$$

$$\frac{5-4}{6} = \frac{62}{T_1}$$

$$T_1 = 62 \times \frac{6}{1} = 372 \text{ K}$$

$$= 372 - 273$$

$$= 100^\circ \text{C}$$

14.

$$\eta = 1 - \frac{T_2}{T_1} = 1 - \frac{127 + 273}{227 + 273} = 1 - \frac{400}{500} = \frac{1}{5}$$

$$\eta = \frac{1}{5} = \frac{W}{Q_{in}}$$

$$W = \frac{1}{5} \times 6 = 1.2 \text{ kcal}$$

$$= 1.2 \text{ kcal}$$

15.

$$\eta = 1 - \frac{T_2}{T_1}$$

$$= 1 - \frac{27 + 273}{127 + 273}$$

$$= 1 - \frac{3}{4}$$

$$= \frac{1}{4}$$

$$\eta = \frac{W}{Q_{in}}$$

$$\frac{1}{4} = \frac{W}{40 \text{ kJ}}$$

$$W = 10 \text{ kJ}$$

16.

$$\eta = \frac{1}{6} = 1 - \frac{T_2}{T_1}$$

$$\frac{T_2}{T_1} = \frac{5}{6}$$

$$\frac{1}{3} = 1 - \frac{T_2 - 62}{T_1}$$

$$\frac{T_2 - 62}{T_1} = \frac{2}{3}$$

$$\frac{T_2}{T_1} - \frac{62}{T_1} = \frac{2}{3}$$

$$\frac{62}{T_1} = \frac{2}{3} + \frac{T_2}{T_1} = \frac{2}{3} + \frac{5}{6}$$

$$= \frac{4+5}{6} = \frac{9}{6}$$

$$\frac{62}{T_1} = \frac{5}{6} - \frac{2}{3}$$

$$\frac{62}{T_1} = \frac{5-4}{6} = \frac{1}{6}$$

$$T_1 = \frac{62 \times 6}{1}$$

$$\Rightarrow T_1 = 372 \text{ K}$$

17. (B)

18. (A)

19. Heated, Mechanic · Electric → Mechanical → Heat

20.

$$\frac{W}{Q_{in}} = 1 - \frac{273}{303} = \frac{30}{303}$$

$$Q_{in} = \frac{303}{30} \times 1 =$$

$$\beta = \frac{T_2}{T_1 - T_2} = \frac{273}{303 - 273} = \frac{273}{30}$$

$$\beta = \frac{\text{Heat extracted } (Q_e)}{\text{Work done}} = \frac{273 \cdot 91}{30}$$

$$(Q_e) \text{ heat extracted} = 9.1$$

$$Q_1 = Q_2 + W \\ = 9.1 + 1 = 10 \text{ J}$$

21.

$$\eta = 1 - \frac{T_2}{T_1}$$

$$\frac{1}{5} = 1 - \frac{T_2}{T_1}$$

$$\frac{T_2}{T_1} = \frac{4}{5}$$

$$\frac{1}{3} = 1 - \frac{T_2 - 50}{T_1}$$

$$\frac{T_2 - 50}{T_1} = \frac{2}{3} \Rightarrow \frac{T_2}{T_1} - \frac{50}{T_1} = \frac{2}{3}$$

$$\frac{4}{5} - \frac{50}{T_1} = \frac{2}{3}$$

$$\frac{50}{T_1} = \frac{4}{5} - \frac{2}{3}$$

$$\frac{50}{T_1} = \frac{2}{15}$$

$$T_1 = 15 \times 25$$

$$T_1 = 375 \text{ K}$$

$$1 - \frac{T_2}{T_1} = \frac{1}{5}$$

$$T_2 = \frac{4}{5} \times 375$$

$$T_2 = 300 \text{ K}$$

23.

$$\eta = 1 - \frac{293}{313}$$

$$= \frac{20}{313} =$$

$$= \frac{20}{313} \times 100 \%$$

$$= 6.4 \%$$

24.

$$\eta = 1 - \frac{T_2}{T_1}$$

$$\text{For } \eta = 1$$

$$T_2 = 0$$

~~T<sub>2</sub> = 0~~

Not possible



25.

$$\eta = 1 - \frac{T_2}{T_1}$$

$$= 1 - \frac{27+273}{677+273}$$

$$= 1 - \frac{300}{950} = \frac{650}{950} = \frac{13}{19}$$

$$\frac{W}{Q_{in}} = \frac{13}{19}$$

$$W = \frac{13}{19} \times 100 \text{ kcal}$$

$$= \frac{13 \times 100 \times 4.2 \times 10^3}{19} \text{ Joules}$$

$$= 0.28 \times 10^6 \text{ Joules}$$

