

UNITS & DIMENSION BOOKLET (SOLUTION)

1. (D)
Theoretical
2. (B)
Impulse = Δp
4. $F = 6\pi\eta r V$
5. $T = \frac{F}{L}$
6. $F = \frac{GM_1M_2}{r^2}$
7. $\frac{d\theta}{dt} = \frac{KA(\Delta T)}{L}$ thermal conductivity
8. $P = e\sigma AT^4$
9. Theoretical
10. Theoretical
11. Theoretical
12. Theoretical
13. Theoretical
14. Theoretical
15. Theoretical
16. $\left(P + \frac{a}{v^2}\right)(v - b) = C T$
 $\frac{a}{v^2}$ must have dimension of pressure
 $M^1L^{-1}T^{-2} = \frac{[a]}{[L^3]^2}$
 $[a] = M^1L^5T^{-2}$
17. $PV = nRT$
 $[R] = \left[\frac{PV}{nT}\right]$
18. Theoretical
19. $E = hv$

$$n = \frac{e}{v}$$

$$M^1 L^2 T^{-1}$$

20. $h = \frac{E}{v}$

Joule second

21. Theoretical

22. $M^a L^b T^c \propto M^a L^b [L^1 T^{-2}]^c$

$$a = 0$$

$$b + c = 0$$

$$1 = -2c$$

$$c = \frac{-1}{2}$$

$$b = \frac{1}{2}$$

23. (B)

$$L^3 \alpha (L^2)^\alpha (L^1 T^{-1})^\beta t^r$$

$$2\alpha + \beta = 3$$

$$-\beta + r = 0$$

$$\beta = r$$

24. $h = \frac{2T \cos \alpha}{rsg}$

25. (D)

M = mass/length

$$ML^{-1}T^0$$

26. (D)

bt dimationless

27. wave velocity

28. $(P) = \left[\frac{a}{v^2} \right]$

$$[a] = [pv^2]$$

29. $[v] = [b]$

30. $nRT = pv$

Energy

31. $ab = [pv^2][v]$

$$[M^1 L^{-1} T^{-2}][L^6][L^3]$$

$$= M^1 L^8 T^{-2}$$

$$32. \quad y = \frac{F'L}{A \Delta L}$$

$$[y] = [FA^2V^{-1}]$$

$$33. \quad F = \frac{q^1 q^2}{4\lambda \epsilon_0 r^2}$$

$$[\epsilon_0] = \frac{[F][R^2]}{[q^2]}$$

$$35. \quad \frac{1}{\sqrt{\mu_0 \epsilon_0}} = v$$

$$36. \quad Q = ms \Delta T$$

$$S = \frac{[Q]}{[m][\Delta T]}$$

$$= \frac{M^1 L^2 T^{-2}}{M K}$$

$$M^0 L^2 T^{-2} K^{-1}$$

$$37. \quad Q = ML$$

$$L = \frac{Q}{M}$$

$$[L] = [M^0 L^2 T^2]$$

38. Theoretical

39. Theoretical

40. Theoretical

$$41. \quad E = \frac{kq}{r^2}$$

42. Theoretical

43. Theoretical

44. Theoretical

45. Theoretical

$$46. \quad M \propto V^a F^b E^c$$

$$[M^1] = [L^1 T^{-1}]^a [M^1 L^1 T^{-2}]^b [M^1 L^2 T^{-2}]^c$$

$$a + b + 2c = 0$$

$$-a - 2b - 2c = 0$$

$$b + c = 1$$

$$2b + 2c = 2$$

$$\begin{aligned}
 -a - 2 &= 0 \\
 -2 + b + 2(1 - b) &= 0 \\
 -2 + b + 2 - 2b &= 0 \\
 b &= 0 \\
 c &= 1 \\
 [M] &= V^{-2} F^0 E^1
 \end{aligned}$$

47. $F \propto \sqrt{T}$
 $Y \propto T$

48. Theoretical

49. Theoretical

50. $[t] = [d]^1 [R]^b [S]^1$
 $T = [M^1 L^3 L^b M^1 L^1 T^{-2} L^{-1}]^{1/2}$
 $L \frac{3+b}{2} = L^0$
 $\frac{3+b}{2} = 0$
 $b = -3$

51. Theoretical

54. $\left[\frac{dp}{dx} \right] = M^1 L^{-2} T^{-2}$

55. Theoretical

56. Theoretical

57. Theoretical

58. Theoretical

59. $M^1 L^2 T^{-2}$
 $[cv^2] = [E]$

60. Theoretical

61. $[S] = [E]^a [V]^b [T]^c$
 $M^1 T^{-2} = [M^1 L^2 T^{-2}]^a [L^1 T^{-1}]^b [T]^c$
 $1 = a$
 $0 = 2a + b$
 $0 = 2$
 $-2 = -2a - b + c$
 $-2 = -2 + 2 + c$
 $c = -2$

62. Theoretical

63. Theoretical

$$65. \frac{\Delta v}{v} = \frac{3\Delta r}{r}$$
$$= 3\%$$

$$66. \frac{\Delta v}{v} = \frac{3\Delta r}{r}$$
$$\frac{6}{3} = \frac{\Delta r}{r}$$
$$\frac{\Delta r}{r} = 2\%$$
$$\frac{\Delta A}{A} = \frac{2\Delta r}{r} = 4\%$$

$$67. \frac{dx}{x} = X \frac{\Delta M}{M} + Y \frac{\Delta L}{L} + Z \frac{\Delta T}{T}$$
$$= ax + by + cz$$

$$68. T = 2z \sqrt{\frac{\ell}{g}}$$
$$T^2 = 4z^2 \frac{\ell}{g}$$
$$g = 4z^2 \frac{\ell}{T^2}$$
$$\frac{\Delta g}{g} = \frac{\Delta \ell}{\ell} + \frac{2\Delta T}{T}$$
$$= 2 + 2 \times 3$$
$$= 8\%$$

WINDOW TO JEE MAIN

1. Torque work
Work = F. S
Torque $r \times F$

2. same as 1

$$3. v = \frac{1}{\sqrt{\mu_0 \epsilon_0}}$$
$$v^2 = \frac{1}{\mu_0 \epsilon_0}$$
$$\left[\frac{1}{\mu_0 \epsilon_0} \right] = [L^2 T^{-2}]$$

4. $F = 6 z \eta r v$

$$[\eta] = \frac{[F]}{[r][v]}$$

$$= \frac{M^1 L^1 T^{-2}}{L^1 L^1 T^{-1}} = M^1 L^{-1} T^{-1}$$

5. Theoretical

6. Theoretical

8. $p = mv$
 $p = 3.513 \times 5.00$
 $= 17.565$
 $= 17.6 \text{ kg ms}^{-1}$

9. Theoretical

10. $LC = \frac{1}{30} \times (0.5^\circ) = \frac{1}{60} = 1 \text{ min}$

11. 5, 1, 2

12. Theoretical

13.

14.

15. Theoretical

16. $T = 2\pi \sqrt{\frac{\ell}{g}}$
 $g = \frac{4\lambda^2 \ell}{T^2}$
 $\frac{\Delta g}{g} = \frac{\Delta \ell}{\ell} + 2 \frac{\Delta T}{T}$
 $= \frac{1}{200} + 2 \times \frac{1}{90}$

17.

18.